This is a 2 hour exam with 200 total marks. No books, notes or calculators. Exam sheet may be retained by student.

**Part I: Basic concepts**

1. [30 marks] State and prove a theorem which makes precise the concept that equivalence relations and partitions are interchangable. Important note [15 marks out of 30]: Give precise definitions of all terms and state the theorem carefully before embarking on the proof.

2. [30 marks total] Prove that a function $f: X \rightarrow Y$ is an isomorphism of sets if and only if $f$ is bijective. Important note [15 marks out of 30]: Give precise definitions of all terms and state the theorem carefully before embarking on the proof.

3. [40 marks total]
   a. [5 marks] Carefully define the field of fractions of an integral domain as a set with operations.
   b. [5 marks] Provide an alternative definition of the field of fractions of an integral domain by a universal property.
   c. [20 marks] Prove carefully that the first definition provides a well defined object.
   d. [10 marks] Prove that the two definitions are equivalent.

**Part II: Commutative and Multilinear Algebra specifics**

Write a clear proposal and description for the ideal masters level course entitled Commutative and Multilinear algebra at University of Melbourne. Be sure to include:

1. [5 marks] Time commitment: Contact hours and total time commitment
2. [5 marks] Prerequisites and recommended background knowledge
3. [5 marks] Subject overview
4. [5 marks] Objectives
5. [5 marks] Assessment
6. [5 marks] Prescribed texts and recommended texts
7. [10 marks] List of topics
8. [60 marks: 5 marks for each of 12 weeks] lecture by lecture schedule (36 lectures) with the topic of each lecture, and a list of the definitions and theorems to be covered in each lecture.